# Periodic Trends in the Edge and Vertex Inversion Barriers for Tricoordinate Pnictogen Hydrides and Fluorides 

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#### Abstract

The edge and vertex inversion barriers for $\mathrm{PH}_{3}, \mathrm{PF}_{3}, \mathrm{AsH}_{3}, \mathrm{AsF}_{3}, \mathrm{SbH}_{3}$, and $\mathrm{SbF}_{3}$ have been calculated by ab initio molecular orbital theory. Large basis sets were employed, and correlation corrections were included at the MP-2 level. The force fields were calculated to identify various transition states. The hydrides invert by a vertex inversion process through a planar trigonal $D_{3 h}$ transition state while the fluorides invert by an edge inversion process through a planar T-shaped $C_{2 v}$ transition state. The vertex inversion barrier heights including zero-point corrections for the hydrides are as follows: $\mathrm{PH}_{3}$, $34.1 \mathrm{kcal} / \mathrm{mol}$; AsH $\mathrm{H}_{3}, 40.6 \mathrm{kcal} / \mathrm{mol}$; and $\mathrm{SbH}_{3}, 42.1 \mathrm{kcal} / \mathrm{mol}$. The edge inversion barriers including zero-point corrections for the fluorides are as follows: $\mathrm{PF}_{3}, 52.9 \mathrm{kcal} / \mathrm{mol} ; \mathrm{AsF}_{3}, 45.7 \mathrm{kcal} / \mathrm{mol}$; and $\mathrm{SbF}_{3}, 38.3 \mathrm{kcal} / \mathrm{mol}$. The vertex inversion barriers for the hydrides increase with increasing pnictogen atomic number while the edge inversion barriers for the fluorides decrease.


We have recently shown ${ }^{1}$ that inversion at pnictogen ${ }^{2}$ centers can proceed via an edge inversion process instead of the vertex inversion process typified by ammonia inversion. Edge inversion can occur if the pnictogen center is substituted by appropriate electronegative groups. The T-shaped transition state for edge inversion, A , can be stabilized by $\sigma$-acceptors in the axial positions

(Ax) and $\pi$-donors in the equatorial (Eq) position. Our initial work focussed on inversion at phosphorus with varying degrees of fluorine substitution. It is of interest to understand the periodic trends as one goes down the pnictogen series. For example, theoretical calculations on the pnictogen hydrides show that the vertex inversion barriers for $\mathrm{AsH}_{3}{ }^{3}$ and $\mathrm{SbH}_{3}{ }^{4}$ are $10-12 \mathrm{kcal} / \mathrm{mol}$ higher than the inversion barrier in $\mathrm{PH}_{3}{ }^{5}$ Furthermore, theoretical work ${ }^{6}$ on the vertex inversion barriers for closed-shell firstand second-row tricoordinate hydrides of the form $\mathrm{AH}_{3}{ }^{-}, \mathrm{AH}_{3}$, $\mathrm{AH}_{3}{ }^{+}$have shown that correlation corrections are small; this is in agreement with Freed's theorem. ${ }^{7}$

[^0]We present ab initio molecular orbital calculations which examine the periodic trends in the inversion barrier for the trifluoro pnictogens $\mathrm{PF}_{3}, \mathrm{AsF}_{3}$, and $\mathrm{SbF}_{3}$. We also examine the effects of correlation on these barriers at the MP- 2 level ${ }^{8}$ and on the barriers for the corresponding hydrides $\mathrm{PH}_{3}, \mathrm{AsH}_{3}$, and $\mathrm{SbH}_{3}$.

## Calculations

Most of the geometries of the $C_{3 c}$ ground states, the $D_{3 h}$ structures (possible vertex inversion transition state), and the $C_{2}$. structures (possible edge inversion transition state) were gradient optimized ${ }^{9}$ at the SCF level with the program HoNDo ${ }^{10}$ on an IBM-3081 computer. If the structures were not optimized with hondo, they were gradient optimized with the program GRADSCF ${ }^{11}$ on a CRAY-1A computer. Force fields and MP- 2 correlation corrections were determined with the rapid analytic techniques incorporated in Gradscf. ${ }^{12}$ Only the valence $s$ and $p$ electrons were incorporated in the MP-2 calculations.

For $\mathrm{PF}_{3}$ and $\mathrm{PH}_{3}$, the geometries were optimized with a $\mathrm{DZ}+\mathrm{P}$ basis set of the form ( $11 \mathrm{~s} 7 \mathrm{p} 1 \mathrm{~d} / 9 \mathrm{~s} 5 \mathrm{pld} / 4 \mathrm{~s} 1 \mathrm{p}$ )/[6s4pld/3s2pld/2s1p] in the order P, F, H. ${ }^{13}$ The $s, p$, and d orbital coefficients are from Dunning and Hay ${ }^{14}$ with $\zeta_{\mathrm{p}}(3 \mathrm{~d})=0.50$. The final force field and energy calculations were done with a slightly larger basis set of the form ( $13 \mathrm{~s} 9 \mathrm{pld} / 9 \mathrm{~s} 5 \mathrm{pld} / 4 \mathrm{slp}$ )/[6s4pld/4s2pld/2slp]. The exponents and coefficients for F and H are from Dunning, ${ }^{15}$ those for P from McLean and Chandler, ${ }^{16}$ and the polarization exponents are those given above. For $\mathrm{AsF}_{3}$ and $\mathrm{SbF}_{3}$, the [ 3 s 2 pld ] basis set for F given above was employed. For $\mathrm{AsH}_{3}$ and $\mathrm{SbH}_{3}$ a ( 5 s 1 p )/[3s1p] basis set on H was employed with $\zeta_{\mathrm{H}}(2 \mathrm{p})=1.0$ as used above. For As the basis set is of better than $\mathrm{DZ}+\mathrm{P}$ quality and has the form ( 14 s 11 p 6 d )/[10s8p3d]. Following previous work, ${ }^{17}$ the exponents and contraction coefficients are from Dunning's compilation. ${ }^{18}$ The first five s orbitals are contracted together,

[^1]Table I. Optimized Geometry Parameters for Pnictogen Hydrides and Fluorides ${ }^{a}$

| property | $\mathrm{PH}_{3}$ | $\mathrm{PF}_{3}$ | $\mathrm{AsH}_{3}$ | $\mathrm{AsF}_{3}$ | $\mathrm{SbH}_{3}$ | $\mathrm{SbF}_{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $r\left(C_{30}\right)$ | $1.407(1.427)^{b}$ | $1.563(1.561)^{b}$ | $1.508(1.511)^{\text {b }}$ | 1.693 (1.709) ${ }^{\text {c }}$ | $1.707(1.710)^{b}$ | $1.874(1.879)^{\text {c }}$ |
| $\theta\left(\mathrm{C}_{3 v}\right)$ | 95.2 (93.3) | 97.1 (97.1) | 94.3 (92.1) | 95.4 (95.9) | 94.3 (91.7) | 93.6 (94) |
| $r\left(D_{3 h}\right)$ | 1.371 | 1.664 | 1.458 | 1.799 | 1.652 | 1.960 |
| $r_{\text {Ax }}\left(C_{2 v}\right)$ | 1.648 | 1.633 | 1.784 | 1.774 | 1.919 | 1.939 |
| $r_{\text {Eq }}\left(C_{2 v}\right)$ | 1.402 | 1.533 | 1.503 | 1.676 | 1.710 | 1.862 |
| $\theta_{A x-P_{n-A x}}\left(C_{2 v}\right)$ | 166.0 | 172.8 | 165.1 | 169.5 | 161.1 | 163.2 |
| $\theta\left(\mathrm{Eq}_{-\mathrm{Pn}-\mathrm{Ax}}\left(C_{2 v}\right)\right)$ | 83.0 | 86.4 | 82.5 | 84.8 | 80.5 | 81.6 |

${ }^{a}$ Bond distances in $\AA$. Bond angles in deg. Experimental values in parentheses. ${ }^{b}$ Reference 18 . ${ }^{〔}$ Reference 19.

Table II. Total Energies (au) for the Pnictogen Hydrides and Fluorides

|  | $\mathrm{E}(\mathrm{SCF})$ | $\mathrm{E}(\mathrm{MP}-2)$ |
| :---: | ---: | :---: |
| $\mathrm{PH}_{3}\left(C_{3 v}\right)$ | -342.475220 | -342.606415 |
| $\mathrm{PH}_{3}\left(D_{3 h}\right)$ | -342.417431 | -342.550655 |
| $\mathrm{PH}_{3}\left(C_{2 v}\right)$ | -342.223498 | -342.351600 |
| $\mathrm{PF}_{3}\left(C_{3 v}\right)$ | -639.240822 | -639.857757 |
| $\mathrm{PF}_{3}\left(D_{3 h}\right)$ | -639.042048 | -639.721743 |
| $\mathrm{PF}_{3}\left(C_{2 v}\right)$ | -639.131879 | -639.772018 |
| $\mathrm{AsH}_{3}\left(C_{3 v}\right)$ | -2235.899263 | -2236.025755 |
| $\mathrm{AsH}_{3}\left(D_{3 k}\right)$ | -2235.831624 | -2235.959956 |
| $\mathrm{AsH}_{3}\left(C_{2 v}\right)$ | -2235.675436 | -2235.799118 |
| $\mathrm{AsF}_{3}\left(C_{3 v}\right)$ | -2532.641874 | -2533.260261 |
| $\mathrm{AsF}_{3}\left(D_{33}\right)$ | -2532.488480 | -2533.154661 |
| $\mathrm{AsF}_{3}\left(C_{2 v}\right)$ | -2532.549859 | -2533.186401 |
| $\mathrm{SbH}_{3}\left(C_{3 v}\right)$ | -6313.979607 | -6314.089471 |
| $\mathrm{SbH}_{3}\left(D_{3 h}\right)$ | -6313.908181 | -6314.021333 |
| $\mathrm{SbH}_{3}\left(C_{2 v}\right)$ | -6313.802356 | -6313.910906 |
| $\mathrm{SbF}_{3}\left(C_{3 v}\right)$ | -6610.755058 | -6611.359512 |
| $\mathrm{SbF}_{3}\left(D_{3 k}\right)$ | -6610.626259 | -6611.267247 |
| $\mathrm{SbF}_{3}\left(C_{2 v}\right)$ | -6610.680916 | -6611.297790 |

as are the first four $p$ orbitals and the first four $d$ orbitals. The remaining orbitals are left variationally free. The exponent of the final d function is 0.3269 obtained by a geometric progression based on the final two d exponents given by Dunning. For Sb , the basis set has the form ( 15 s 11 p 8 d )/[10s7p5d] and was constructed in a similar fashion again from an atomic basis set of Dunning. ${ }^{19}$ On the basis of the previous work on $\mathrm{GeH}_{4},{ }^{17}$ we only contracted the first six $s$ functions, the first five p orbitals, and the first four d orbitals. The final d orbital exponent was 0.247 obtained as described above.

## Results and Discussion

The optimized geometry parameters are given in Table I, while the total energies are given in Table II. The experimental geometries for the pyramidal $C_{3 v}$ structures have all been reported in the literature, ${ }^{20,21}$ The bond lengths for $\mathrm{PH}_{3}$ and $\mathrm{AsH}_{3}$ are shorter than the experimental values by 0.020 and $0.003 \AA$, respectively. The error for $\mathrm{PH}_{3}$ is typical of that found for large basis set SCF calculations while the difference for $\mathrm{AsH}_{3}$ is somewhat smaller than normally found. The bond distance for $\mathrm{SbH}_{3}$ is also calculated to be $0.003 \AA$ less than the experimental value. The bond angle is $1.9^{\circ}$ too large for $\mathrm{PH}_{3}$ and $2.2^{\circ}$ too large for $\mathrm{AsH}_{3}$. The difference increases to $2.6^{\circ}$ for $\mathrm{SbH}_{3}$. Previous SCF-CI calculations on $\mathrm{PH}_{3}{ }^{4}$ have shown that the bond distances for $\mathrm{PH}_{3}$ increase and that the bond angles decrease when correlation corrections are included.

The $\mathrm{Pn}-\mathrm{H}$ bond distances decrease in the $D_{3 h}$ structure of the hydrides as expected if the lone pair is in the out-of-plane porbital of $\mathrm{a}_{2}{ }^{\prime \prime}$ symmetry. The magnitude of the decrease in the $\mathrm{Pn}-\mathrm{H}$ bond distances increases with increasing atomic number, for $\mathrm{PH}_{3}$, $-0.036 \AA$; for $\mathrm{AsH}_{3},-0.050 \AA$; and for $\mathrm{SbH}_{3},-0.055 \AA$.

The T-shaped $C_{2 v}$ structures for the hydrides show very long bonds from the pnictogen to the axial hydrogens and essentially no change in the equatorial $\mathrm{Pn}-\mathrm{H}$ bond distance. The increases for the Pn -Ax bond distances are $0.241 \AA$ for $\mathrm{PH}_{3}, 0.276 \AA$ for $\mathrm{AsH}_{3}$, and $0.212 \AA$ for $\mathrm{SbH}_{3}$. The $\mathrm{Ax}-\mathrm{Pn}-\mathrm{Ax}$ bond angles are

[^2]all less than $180^{\circ}$ and decrease with increasing pnictogen atomic number from 166.0 for $\mathrm{PH}_{3}$ to 161.1 for $\mathrm{SbH}_{3}$. As a consequence, a plane which includes the pnictogen center and is normal to the equatorial bond-lone pair axis separates all of the substituents from the lone pair.


The optimized bond distances for the fluorides agree well with the experimental values. For $\mathrm{PF}_{3}$, the calculated value is 0.002 $\AA$ longer than the experimental equilibrium value ${ }^{20}$ while for $\mathrm{AsF}_{3}$ the calculated value is $0.016 \AA$ shorter. ${ }^{21}$ For $\mathrm{SbF}_{3},{ }^{21}$ the calculated value is only $0.005 \AA$ shorter. For the fluorides, the calculated values for $\theta(\mathrm{FPnF})$ are slightly smaller than the experimental values, $0.6^{\circ}$ for $\mathrm{PF}_{3}$ and $0.5^{\circ}$ for $\mathrm{AsF}_{3}$.

The $\mathrm{Pn}-\mathrm{F}$ bond lengths increase in the planar $D_{3 h}$ structures as compared to the pyramidal $C_{3 v}$ structures (contrary to the decrease observed for the hydrides). For $\mathrm{PF}_{3}$ this increase is 0.101 $\AA$, for $\mathrm{AsF}_{3}$ it is $0.106 \AA$, and for $\mathrm{SbF}_{3}$ it is $0.086 \AA$. This is a result of the orbital occupancy in the $D_{3 h}$ structure for $\mathrm{PnF}_{3}$ which places the lone pair in a delocalized $s$ orbital of $a_{1}{ }^{\prime}$ symmetry, not in an out-of-plane $p$ orbital of $a_{2}{ }^{\prime \prime}$ symmetry. This in-plane lone pair leads to increased repulsions with the bond orbitals causing the bond distances to increase. Indeed as shown below the $D_{3 h}$ structures are not minima or even transition states and will become $C_{2 v}$ structures.
The geometries of the T-shaped $C_{2 c}$ structures for the fluorides differ from those observed for the hydrides. The Pn-Ax bonds are longer than those in the pyramidal $C_{3 v}$ form by only 0.070 $\AA$ for $\mathrm{PF}_{3}, 0.081 \AA$ for $\mathrm{AsF}_{3}$, and by $0.065 \AA$ for $\mathrm{SbF}_{3}$; these differences are much smaller than those found in the hydride series. The $\mathrm{Pn}-\mathrm{Eq}$ bond lengths are now shorter than the $C_{3 c}$ distances by $0.030 \AA$ for $\mathrm{PF}_{3}, 0.017 \AA$ for $\mathrm{AsF}_{3}$, and $0.014 \AA$ for $\mathrm{SbF}_{3}$. The $\mathrm{Ax}-\mathrm{Pn}-\mathrm{Ax}$ bond angles are again all less than $180^{\circ}$ and are larger than those in the corresponding hydrides. These bond angles show the same periodic trend of a decrease with increasing pnictogen atomic number as found for the hydrides.

In order to assess whether the calculated structures are minima or transition states and to determine the magnitude of the zeropoint corrections to the barrier heights, the molecular force fields were determined analytically. We present here only the zero-point energies and the number of imaginary frequencies for each structure in Table III. As expected, the pyramidal $C_{30}$ structures are all minima on the surface with no imaginary frequencies. For the hydrides, the $D_{3 h}$ structures are transition states characterized by one imaginary frequency corresponding to the vertex inversion mode. The T-shaped $C_{2 i}$ structures of the hydrides with the lone pair in the molecular plane correspond to minima on their appropriate energy hypersurfaces (see below). For the fluorides, the T-shaped $C_{2}$ structures are transition states with one imaginary frequency corresponding to the edge inversion motion discussed earlier. The $D_{3 h}$ structures with an $\mathrm{a}_{1}{ }^{\prime} \mathrm{s}$ orbital lone pair have three imaginary frequencies and are thus not even saddle points. The most appropriate description is that they are high-energy forms (distorted) of the $C_{2 v}$ structures which is confirmed by the normal modes for the imaginary frequencies. There is, of course,

Table III. Zero-Point Energies and Number of Imaginary Frequencies for the Prictogen Hydrides and Fluorides

| molecule | $\mathrm{ZPE}^{a}(\mathrm{kcal} / \mathrm{mol})$ | no. imaginary $\nu$ | $i v\left(\mathrm{~cm}^{-1}\right)$ |
| :--- | :---: | :---: | :--- |
| $\mathrm{PH}_{3}\left(C_{3 v}\right)$ | $16.19(14.58)^{b}$ | 0 |  |
| $\mathrm{PH}_{3}\left(D_{3 h}\right)$ | 15.18 | 1 | $1238 i$ |
| $\mathrm{PH}_{3}\left(C_{2 v}\right)$ | 14.43 | 0 |  |
| $\mathrm{PF}_{3}\left(C_{3 v}\right)$ | $5.83(5.41)^{b}$ | 0 |  |
| $\mathrm{PF}_{3}\left(D_{3 h}\right)$ | 2.63 | 3 | $827 i, 308 i\left(\mathrm{E}^{\prime}\right)$ |
| $\mathrm{PF}_{3}\left(C_{2 v}\right)$ | 4.81 | 1 | $365 i$ |
| $\mathrm{AsH}_{3}\left(C_{3 v}\right)$ | $14.69(13.25)^{b}$ | 0 |  |
| $\mathrm{AsH}_{3}\left(D_{3 h}\right)$ | 13.90 | 1 | $1235 i$ |
| $\mathrm{AsH}_{3}\left(C_{2 v}\right)$ | 13.14 | 0 |  |
| $\mathrm{AsF}_{3}\left(C_{3 v}\right)$ | $4.66(4.31)^{c}$ | 0 |  |
| $\mathrm{AsF}_{3}\left(D_{3 h}\right)$ | 2.45 | 3 | $492 i, 201 i\left(\mathrm{E}^{\prime}\right)$ |
| $\mathrm{AsF}_{3}\left(C_{2 v}\right)$ | 3.96 | 1 | $263 i$ |
| $\mathrm{SbH}_{3}\left(C_{3 v}\right)$ | $12.88(11.60)^{b}$ | 0 |  |
| $\mathrm{SbH}_{3}\left(D_{3 h}\right)$ | 12.10 | 1 | $1128 i$ |
| $\mathrm{SbH}_{3}\left(C_{2 v}\right)$ | 13.26 | 0 |  |
| $\mathrm{SbF}_{3}\left(C_{3 v}\right)$ | 4.08 | 0 |  |
| $\mathrm{SbF}_{3}\left(D_{3 h}\right)$ | 2.41 | 3 | $356 i, 150 i\left(\mathrm{E}^{\prime}\right)$ |
| $\mathrm{SbF}_{3}\left(C_{2 v}\right)$ | 3.60 | 1 | $199 i$ |

${ }^{a}$ Experimental values in parentheses. ${ }^{b}$ Reference $20{ }^{\text {}}$ Reference 21.
an out-of-plane mode, and the two in-plane bends lead to the $C_{2 v}$ structure.

The imaginary inversion frequencies for the inversion motion show different periodic trends. For the hydrides, the imaginary inversion frequencies for $\mathrm{PH}_{3}$ and $\mathrm{AsH}_{3}$ for the $D_{3 h}$ structure are essentially the same. The inversion frequencies at the $C_{30}$ structure differ significantly- $\mathrm{PH}_{3}: 1113 \mathrm{~cm}^{-1}$ (calcd), $992 \mathrm{~cm}^{-1}$ (expt); ${ }^{22}$ and $\mathrm{AsH}_{3}: 1020 \mathrm{~cm}^{-1}$ (calcd), $906 \mathrm{~cm}^{-1}$ (expt). ${ }^{22}$ The imaginary frequency for the inversion motion is higher than the $C_{30}$ inversion frequency. For $\mathrm{SbH}_{3}$, the imaginary frequency at the $D_{3 h}$ structure decreases but is still significantly above the $C_{3 v}$ inversion frequency: $889 \mathrm{~cm}^{-1}$ (calcd), $782 \mathrm{~cm}^{-1}$ (expt). ${ }^{22}$ Thus the transition states are actually tighter in the harmonic approximation for this mode than the ground states.

For the fluorides, the imaginary frequencies for the $C_{2 v}$ structure show a clear periodic trend, decreasing with increasing pnictogen atomic number. Due in part to increased masses of the fluorines, the frequencies are significantly lower in the fluorides than in the hydrides. The imaginary frequency in the fluorides is slightly lower than that for the degenerate bend to which it corresponds in the $C_{3 v}$ structure- $\mathrm{PF}_{3}: 374 \mathrm{~cm}^{-1}$ (calcd), $344 \mathrm{~cm}^{-1}$ (expt); ;2 $\mathrm{AsF}_{3}$ : $287 \mathrm{~cm}^{-1}$ (calcd), $262 \mathrm{~cm}^{-1}$ (expt); ${ }^{23}$ and $\mathrm{SbF}_{3} 222 \mathrm{~cm}^{-1}$ (calcd).

In order to correct the calculated inversion barriers for zeropoint effects, it is necessary to scale the calculated differences in the zero-point energies ( $\triangle Z P E$ ). The calculated frequencies are too high due to neglect of correlation effects and anharmonic effects. For the hydrides, the scale factor for the $C_{3 v}$ structures is 0.90 for all three structures. For $\mathrm{PF}_{3}$ and $\mathrm{AsF}_{3}$ the scale factor is 0.925 and this was used for $\mathrm{SbF}_{3}$.

From our geometric results, it is apparent that the hydrides invert through a planar $D_{3 h}$ transition state representing vertex inversion while the fluorides invert through a T-shaped $C_{20}$ transition state representing edge inversion based solely on the number of imaginary frequencies. This is shown very explicitly by the energetics in Table IV. The hydrides clearly do not invert by the edge inversion process since the $C_{2 v}$ structures are clearly much higher in energy than the corresponding $D_{3 h}$ vertex inversion transition states. (In fact the $C_{2 v}$ structures with an in-plane lone pair are above the $\mathrm{Pn}-\mathrm{H}$ bond strengths. ${ }^{24}$ ) For the hydrides, the barriers to inversion are expected to show an increase with increasing atomic number of the pnictogen although the differences get smaller as the pnictogens get larger. There is also not as large a difference among the three pnictogens $\mathrm{P}, \mathrm{As}$, and Sb as compared

[^3]Table IV. Calculated Inversion Barriers ( $\mathrm{kcal} / \mathrm{mol}$ ) for Pnictogen Hydrides and Fluorides ${ }^{a}$

|  | vertex |  | edge |  |  |
| :---: | ---: | :---: | ---: | ---: | ---: |
| molecule | SCF | MP-2 |  | SCF | MP-2 |
| $\mathrm{PH}_{3}$ | 36.3 | $\underline{35.0}$ |  | 158.0 | 159.9 |
| $\mathrm{PF}_{3}$ | 124.7 | 85.3 | 68.4 | $\underline{53.8}$ |  |
| $\mathrm{AsH}_{3}$ | 42.4 | $\underline{41.3}$ | 140.5 | 142.2 |  |
| $\mathrm{AsF}_{3}$ | 96.3 | 66.3 | 57.7 | $\underline{46.3}$ |  |
| $\mathrm{SbH}_{3}$ | 44.8 | $\underline{42.8}$ | 111.2 | 112.0 |  |
| $\mathrm{SbF}_{3}$ | 80.8 | 57.9 | 46.5 | $\underline{38.7}$ |  |

${ }^{a}$ Underlined values represent the best values for $\Delta E_{0}$ used in determining the barrier heights.
to the difference in barrier heights between $\mathrm{NH}_{3}{ }^{6 \mathrm{~b}}$ and $\mathrm{PH}_{3} .{ }^{5}$ As expected from previous work, correlation corrections lower the barrier heights by $1-2 \mathrm{kcal} / \mathrm{mol}$. This very small correlation effect is excellent agreement with Freed's theorem.?

The energies of the T-shaped $C_{2 v}$ structures for the hydrides also show very small effects due to correlation corrections. In this case, the energies increase by $1-2 \mathrm{kcal} / \mathrm{mol}$. The periodic behavior of the energies of these structures is more pronounced with a large decrease in energy as the pnictogen atomic number increases.

There are a number of previous calculations on the vertex inversion barriers of the hydrides. The best calculated $\Delta E^{5}$ for $\mathrm{PH}_{3}$ is $34.4 \mathrm{kcal} / \mathrm{mol}$ determined from a near Hartree-Fock basis set of STO's and including correlation correction at the CI-SD with a correction for quadruple excitation (CI-SDQ). Our value of $35.0 \mathrm{kcal} / \mathrm{mol}$ is in excellent agreement considering that our basis set is smaller, our correlation correction is simpler, and our use of SCF geometries. For $\mathrm{AsH}_{3}$, the previous calculation ${ }^{3}$ was done at the SCF level with a large STO DZ + P basis set and estimated geometries. The calculated barrier of $46.4 \mathrm{kcal} / \mathrm{mol}$ is in reasonable agreement with our SCF value of $42.4 \mathrm{kcal} / \mathrm{mol}$. Our basis set is somewhat better in the valence space, and our geometries are better in the SCF limit. The correlation correction is again small. The inversion barrier for $\mathrm{SbH}_{3}$ was calculated ${ }^{4}$ previously with an STO basis set that was of minimum basis set quality in the inner shells and of $\mathrm{DZ}+\mathrm{P}$ quality in the valence space. The barrier at this level was $46.2 \mathrm{kcal} / \mathrm{mol}$ as compared to our slightly lower barrier of $44.8 \mathrm{kcal} / \mathrm{mol}$.

The $\Delta$ ZPE corrections are $0.7-0.9 \mathrm{kcal} / \mathrm{mol}$ and give final inversion barriers of $34.1,40.6$, and $42.1 \mathrm{kcal} / \mathrm{mol}$ at the MP- 2 level. For $\mathrm{PH}_{3}$, the best value for the inversion barrier is 33.5 by using our $\triangle$ ZPE correction and the previous CI-SDQ calculation. For $\mathrm{AsH}_{3}$ and $\mathrm{SbH}_{3}$ our values represent the best available values for these barrier heights.

The fluorides clearly will invert through the T-shaped $C_{2 v}$ transition state for edge inversion. Previous work on $\mathrm{PF}_{3}{ }^{25,26}$ has shown that the lowest energy $D_{3 h}$ structure has an sorbital lone pair of $a_{1}{ }^{\prime}$ symmetry with the state with the $p$ orbital lone pair of $\mathrm{a}_{2}{ }^{\prime \prime}$ symmetry $55 \mathrm{kcal} / \mathrm{mol}$ higher in energy. This has also been found in $\mathrm{AsF}_{3}$ where the energy difference is $59 \mathrm{kcal} / \mathrm{mol}$. ${ }^{27}$ Our work clearly demonstrates that the T -shaped $C_{2 v}$ transition state for edge inversion is of lower energy than the $D_{3 h}$ structure with $\mathrm{a}_{1}$ 's orbital occupancy for the lone pair, and, in fact, this $D_{3 h}$ structure is simply a high-energy form of the $C_{2 v}$ structure. The edge inversion barriers for the fluorides show a much larger correlation correction in the direction of decreasing the barrier height than do the vertex inversion barriers of the hydrides. For $\mathrm{PF}_{3}$ the MP- 2 correlation correction is $21 \%$ of the SCF barrier height, for $\mathrm{AsF}_{3}$ it is $20 \%$, and for $\mathrm{SbF}_{3}$ it is $17 \%$. For the hydrides, the correlation corrections are $2-5 \%$ of the SCF value. The correlation correction for the edge inversion process for the fluorides thus does not appear to follow the conclusions usually derived from Freed's theorem. ${ }^{7}$ The large correlation effects for the $C_{2 v}$ structures are consistent with previous estimates ${ }^{25 b}$ based on simple calculations on the inversion barrier for $\mathrm{PF}_{3}$. The

[^4]fluorides also show the opposite periodic trend in the inversion barriers with $\mathrm{SbF}_{3}$ having the lowest edge inversion barrier. Thus the barriers decrease with increasing pnictogen atomic number, and, in fact, the difference is approximately constant in contrast to the leveling effect observed for the hydrides. The $\triangle Z P E$ correction to the edge inversion barriers for the fluorides is again small being $-0.9 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{PF}_{3},-0.6 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{AsF}_{3}$, and $-0.4 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{SbF}_{3}$. The final corrected, correlated barriers for edge inversion in the fluorides are $52.9,45.7$, and $38.3 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{PF}_{3}, \mathrm{AsF}_{3}$, and $\mathrm{SbF}_{3}$, respectively. It is of interest to note that the edge inversion barrier for $\mathrm{SbF}_{3}$ is actually lower than the vertex inversion barrier for $\mathrm{SbH}_{3}$.

The decrease in the edge inversion barrier with increasing pnictogen atomic number is not surprising and correlates well with the increasing stability for increasing pnictogen atomic number observed for ADPnO complexes which have a T-shaped structure. ${ }^{28}$

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Our SCF inversion barrier for $\mathrm{PF}_{3}$ for vertex inversion through the $D_{3 h}$ transition state is in reasonable agreement with the value found by Marynick ${ }^{25 \mathrm{a}}$ of $121.5 \mathrm{kcal} / \mathrm{mol}$ considering the differences in geometries and basis sets. For AsF ${ }_{3}$, our SCF calculation is with a much larger basis set and with much better geometries. Marynick's value ${ }^{27}$ of $111.9 \mathrm{kcal} / \mathrm{mol}$ is $15.6 \mathrm{kcal} / \mathrm{mol}$ higher in energy than our value showing the necessity of a good basis set and a good set of geometries in these calculations.

Finally, returning to the observation that the T -shaped $C_{2 t}$ structures for the hydrides are minima on a potential energy hypersurface, ${ }^{29}$ we note that these structures may be accessed by electronic excitation. Including corrections for $\triangle Z P E$, the $0-0$ transition of these states are calculated to be at 158.1 ( 55,335 $\left.\mathrm{cm}^{-1}\right), 140.6\left(49,210 \mathrm{~cm}^{-1}\right)$, and $112.4\left(39,340 \mathrm{~cm}^{-1}\right) \mathrm{kcal} / \mathrm{mol}$ above the ground state. The observed absorption spectra ${ }^{30}$ are quite complex and have been assigned to Rydberg transitions. We do note that the continuous absorption in $\mathrm{PH}_{3}$ has the maximum intensity at $1800 \AA\left(55,556 \mathrm{~cm}^{-1}\right)$ which is in an energy region consistent with our result. However, for $\mathrm{AsH}_{3}$, the maximum is at $1830 \AA\left(54,645 \mathrm{~cm}^{-1}\right)$ which is higher than our result. For $\mathrm{SbH}_{3}$, the continuum has a maximum intensity at $1970 \AA(50$, $781 \mathrm{~cm}^{-1}$ ), clearly much higher than our value. However, it would seem useful to reinvestigate the UV spectra of these hydrides to look for evidence of the states having $C_{2 v}$ structure.
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# Steric Effects on Atropisomerism in Tetraarylporphyrins 

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#### Abstract

The rate of aryl ring rotation in a series of 5,10,15,20-tetrakis(2-X-5-methoxyphenyl)porphyrins, where $\mathrm{X}=\mathrm{H}$, $\mathrm{F}, \mathrm{Cl}, \mathrm{Br}$, and I , was studied by NMR spectroscopy and chromatography. Where $\mathrm{X}=\mathrm{Cl}, \mathrm{Br}$, and I , the four atropisomers $\alpha \beta \alpha \beta, \alpha \alpha \beta \beta, \alpha \alpha \alpha \beta$, and $\alpha \alpha \alpha \alpha$ were isolated and were stable at 298 K . When $\mathrm{X}=\mathrm{H}$ or F , facile interconversion of the atropisomers at 298 K prevented isolation of pure atropisomers, but for $\mathrm{X}=\mathrm{F}$ samples of $>80 \%$ isomeric purity were isolated at low temperatures. The approach of nonequilibrated mixtures of atropisomers to equilibrium at elevated temperatures was monitored by HPLC experiments for $\mathrm{X}=\mathrm{Cl}, \mathrm{Br}$, and I , and ${ }^{19} \mathrm{~F}$ NMR spectroscopy for $\mathrm{X}=\mathrm{F}$. Rate constants were obtained for the six processes by which the atropisomers can interconvert. The rotational barriers increased monotonically as the van der Waals radii of the substituent X . The rotational barriers were correlated with the "apparent overlap" of the ortho substituents, $\Sigma r^{*}$, a geometric parameter previously proposed to quantify steric interactions on the internal rotation in biaryls.


Biphenyl-type atropisomerization in ortho-substituted tetraphenylporphyrins was first reported by Gottwald and Ullmann ${ }^{1}$ who separated the atropisomers of $5,10,15,20$-tetrakis (ohydroxyphenyl)porphyrin. X-ray structures of several 5,10,15,20-tetraarylporphyrins show that the aryl rings are inclined roughly perpendicular $\left(60-90^{\circ}\right)$ to the plane of the porphyrin ring in both free-base and metallo derivatives in the solid state, ${ }^{2}$ and thus the ortho substituents project above and below the porphyrin plane. Aryl ring rotation in solution has been shown to be slow
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on the NMR time scale at ambient temperature, and the aryl ring, on average, is orthogonal to the plane of the porphyrin. ${ }^{3}$ The atropisomerism, due to restricted rotation of the aryl rings about the porphyrin-arene bond, gives rise to four atropisomers (e.g., Figure 1). In an equilibrated mixture the four atropisomers $\alpha \beta \alpha \beta$, $\alpha \alpha \beta \beta, \alpha \alpha \alpha \beta$, and $\alpha \alpha \alpha \alpha$ are present in the statistical ratio of 1:2:4:1, respectively.

The restricted rotation which results when an amido substituent is placed on the ortho positions of the meso aryl rings has been exploited in the design and synthesis of a number of chemical models for heme-containing biological systems. ${ }^{4}$ On the basis

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